Higher: Straight Line

Revision

1. A line L is perpendicular to the line with equation 2x - 3y - 6 = 0. What is the gradient of the line L?

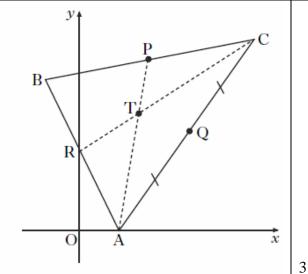
) PI

- A $-\frac{3}{2}$
- B $-\frac{1}{2}$
- $C = \frac{2}{3}$
- D 2

Ans A

21. Triangle ABC has vertices A(4, 0), B(-4, 16) and C(18, 20), as shown in the diagram opposite.

Medians AP and CR intersect at the point T(6, 12).



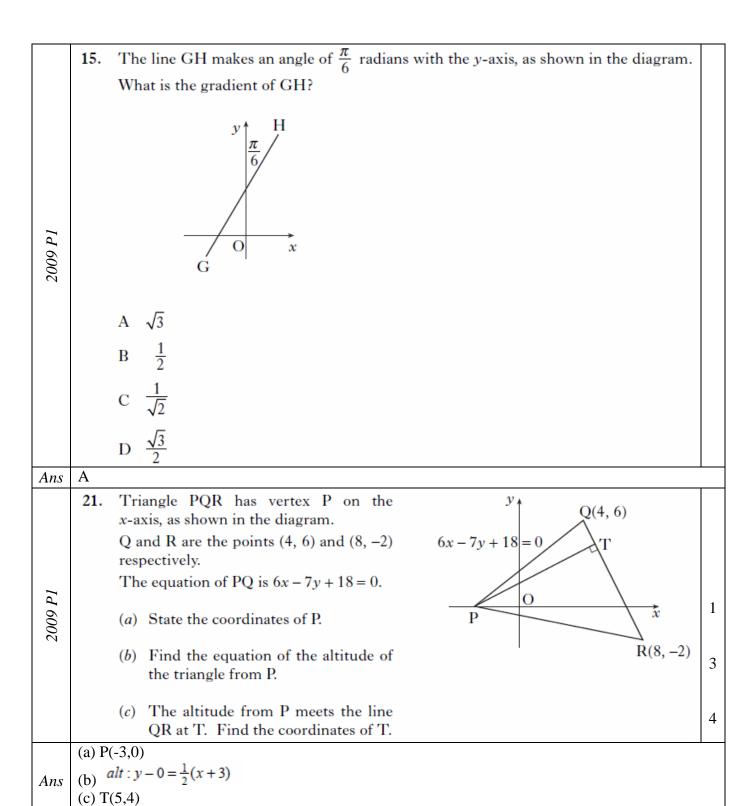
- (a) Find the equation of median BQ.
- (b) Verify that T lies on BQ.
- (c) Find the ratio in which T divides BQ.

2

1

- Ans (a) $y-16 = -\frac{2}{5}(x-(-4))$ or $y-10 = -\frac{2}{5}(x-11)$
 - (b) e.g. Substitution: 2(6) + 5(12) = 12 + 60 = 72
 - (c) 2:1

	3.	Triangle PQR has vertices at P(-3, -2), Q(-1, 4) and R(3, 6).
		PS is a median. What is the gradient of PS?
		A -2
2009 PI		$B -\frac{7}{4}$
		C 1
		$D = \frac{7}{4}$
Ans	D	
	5.	Here are two statements about the points $S(2, 3)$ and $T(5, -1)$:
2009 P I		(1) The length of $ST = 5$ units;
		(2) The gradient of $ST = \frac{4}{3}$.
		Which of the following is true?
200		A Neither statement is correct.
		B Only statement (1) is correct.
		C Only statement (2) is correct.
		D Both statements are correct.
Ans	В	



The diagram shows a circle, centre (2, 5) and a tangent drawn at the point (7, 9). 5. What is the equation of this tangent?

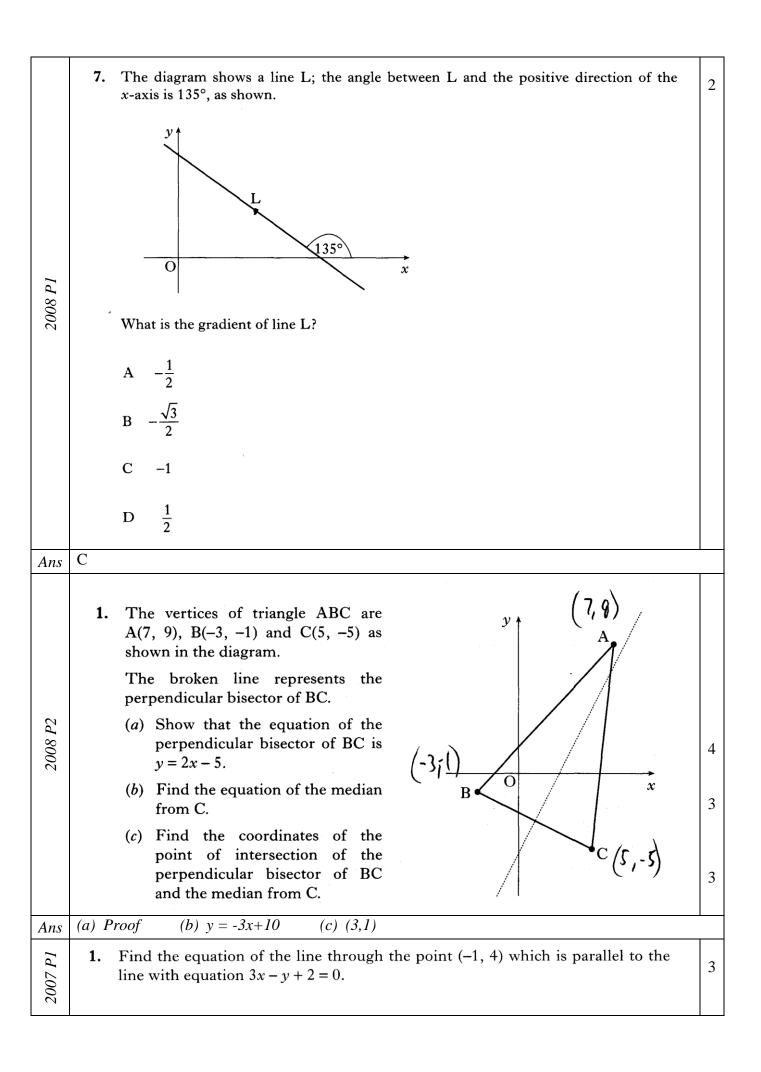
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2008 PI

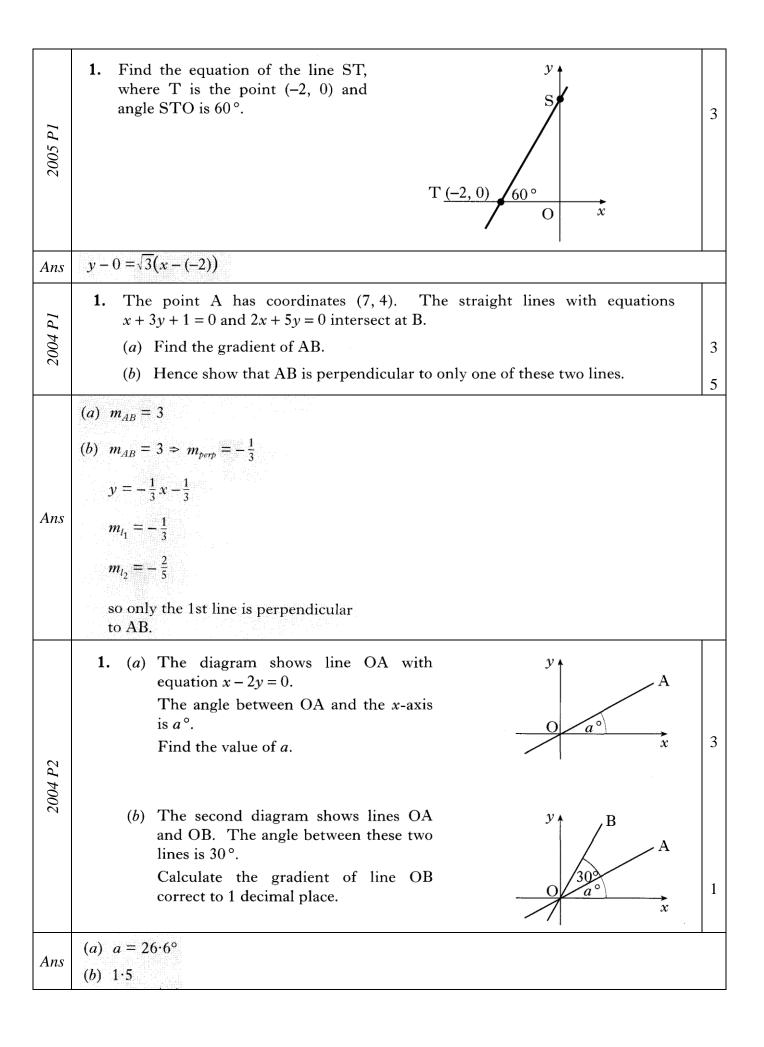
- A $y-9=-\frac{5}{4}(x-7)$
- B $y+9=-\frac{4}{5}(x+7)$
- C $y-7=\frac{4}{5}(x-9)$
- D $y+9=\frac{5}{4}(x+7)$

Ans

A



Ans	y = 3x + 7	
2006 P.I	1. Triangle ABC has vertices A(-1, 12), B(-2, -5) and C(7, -2). (a) Find the equation of the median BD. (b) Find the equation of the altitude AE. (c) Find the coordinates of the point of intersection of BD and AE.	3 3 3
Ans	(a) $y-5=2(x-3)$ or $y+5=2(x-(-2))$ etc (b) $y-12=-3(x-(-1))$ (c) (2, 3)	
2006 P2	 PQRS is a parallelogram. P is the point (2, 0), S is (4, 6) and Q lies on the x-axis, as shown. The diagonal QS is perpendicular to the side PS. (a) Show that the equation of QS is x + 3y = 22. (b) Hence find the coordinates of Q and R. 	4 2
Ans	(a) proof $m_{PS} = 3$ $m_{QS} = -\frac{1}{3}$ $y - 6 = -\frac{1}{3}(x - 4)$ (b) Q = (22, 0) R = (24, 6)	



2003 PI	1. Find the equation of the line which passes through the point (-1, 3) and is perpendicular to the line with equation $4x + y - 1 = 0$.	3			
Ans	s x - 4y + 13 = 0				
PI	1. (a) Find the equation of the straight line through the points $A(-1, 5)$ and $B(3, 1)$.	2			
2002W PI	(b) Find the size of the angle which AB makes with the positive direction of the x-axis.	2			
Ans	(a) $y + x = 4$				
	(b) 135°				
2002W P2	 The diagram shows a rhombus PQRS with its diagonals PR and QS. PR has equation y = 2x - 2. Q has coordinates (-2, 4). (a) (i) Find the equation of the diagonal QS. (ii) Find the coordinates of T, the point of intersection of PR and QS. (b) R is the point (5, 8). Write down the coordinates of P. 	6			
Ans	(a) $2y + x = 6$, T(2, 2) (b) P(-1, -4)				
2002 P2	 Triangle ABC has vertices A(-1, 6), B(-3, -2) and C(5, 2). Find (a) the equation of the line p, the median from C of triangle ABC. (b) the equation of the line q, the perpendicular bisector of BC. (c) the coordinates of the point of intersection of the lines p and q. 	3 4 1			
Ans	(a) $y = 2$				
	(b) y = -2x + 2				
	(c) $(0, 2)$				

2001 PI	1. Find the equation of the straight line which is parallel to the line with equation $2x + 3y = 5$ and which passes through the point $(2, -1)$.	3
Ans	2x + 3y = 1	
2001 P2	 7. Triangle ABC has vertices A(2, 2), B(12, 2) and C(8, 6). (a) Write down the equation of l₁, the perpendicular bisector of AB. (b) Find the equation of l₂, the perpendicular bisector of AC. (c) Find the point of intersection of lines l₁ and l₂. (d) Hence find the equation of the circle passing through A, B and C. 	1 4 1 2
Ans	(a) $x = 7$ (b) $3x + 2y = 23$ (c) $(7, 1)$ (d) $(x - 7)^2 + (y - 1)^2 = 26$ 3. Find the size of the angle a° that the	
2000 PI	line joining the points $A(0, -1)$ and $B(3\sqrt{3}, 2)$ makes with the positive direction of the x-axis. $A(0, -1)$	3
Ans	30 degrees	
2000 P2	2. (a) Find the equation of AB, the perpendicular bisector of the line joining the points P(-3, 1) and Q(1, 9).	4

Ans	(a) x + 2y = 9	
Specimen 2 PI	2. A and B are the points (-3, -1) and (5, 5). Find the equation of the perpendicular bisector of AB. B (5, 5) A (-3, -1)	4
Ans	$m_{AB} = \frac{3}{4} \Rightarrow m_{perp} = -\frac{4}{3}$ midpoint = (1,2) $y - 2 = -\frac{4}{3}(x - 1)$	
Specimen 2 PI	4. The line AB makes an angle of $\frac{\pi}{3}$ radians with the y-axis, as shown in the diagram. Find the exact value of the gradient of AB.	2
Ans	angle between line and x-axis = $\frac{\pi}{2} - \frac{\pi}{3}$ gradient = $\tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}$	
Specimen 1 P1	1. P(-4, 5), Q(-2, -2) and R(4, 1) are the vertices of triangle PQR as shown in the diagram. Find the equation of PS, the altitude from P. P(-4, 5) P(-4, 5) P(-4, 5) P(-4, 5)	3
Ans	y = -2x - 3	
Specimen 1 P2	1. ABCD is a parallelogram. A, B and C have coordinates (2, 3), (4, 7) and (8, 11). Find the equation of DC.	3
Ans	y = 2x - 5	