## X100/201

NATIONAL
QUALIFICATIONS 2007

TUESDAY, 15 MAY
$1.00 \mathrm{PM}-1.45 \mathrm{PM}$

# MATHEMATICS 

INTERMEDIATE 2
Units 1, 2 and 3
Paper 1
(Non-calculator)

## Read carefully

1 You may NOT use a calculator.
2 Full credit will be given only where the solution contains appropriate working.
3 Square-ruled paper is provided.

## FORMULAE LIST

The roots of $a x^{2}+b x+c=0$ are $x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

Sine rule: $\quad \frac{a}{\sin \mathrm{~A}}=\frac{b}{\sin \mathrm{~B}}=\frac{c}{\sin \mathrm{C}}$

Cosine rule: $\quad a^{2}=b^{2}+c^{2}-2 b c \cos \mathrm{~A}$ or $\cos \mathrm{A}=\frac{b^{2}+c^{2}-a^{2}}{2 b c}$

Area of a triangle: $\quad$ Area $=\frac{1}{2} a b \sin \mathrm{C}$

Volume of a sphere: $\quad$ Volume $=\frac{4}{3} \pi r^{3}$

Volume of a cone: $\quad$ Volume $=\frac{1}{3} \pi r^{2} h$

Volume of a cylinder: $\quad$ Volume $=\pi r^{2} h$

Standard deviation: $\quad s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}=\sqrt{\frac{\sum x^{2}-\left(\sum x\right)^{2} / n}{n-1}}$, where $n$ is the sample size.

ALL questions should be attempted.

1. The table below shows the results of a survey of First Year pupils.

|  | Wearing a blazer | Not wearing a blazer |
| :--- | :---: | :---: |
| Boys | 40 | 22 |
| Girls | 29 | 9 |

What is the probability that a pupil, chosen at random from this sample, will be a girl wearing a blazer?
2.


Find the equation of the straight line passing through the points $(0,-3)$ and $(-2,-11)$.
3. A tin of tuna is in the shape of a cylinder.


It has diameter 10 centimetres and height 4 centimetres.
Calculate its volume.
Take $\boldsymbol{\pi}=\mathbf{3 \cdot 1 4}$.
4. Find the point of intersection of the straight lines with equations $x+2 y=-5$ and $3 x-y=13$.
5. Multiply out the brackets and collect like terms.

$$
(x+3)\left(x^{2}+4 x-12\right)
$$

6. (a) Show that the standard deviation of $1,1,1,2$ and 5 is equal to $\sqrt{ } 3$.
(b) Write down the standard deviation of 101, 101, 101, 102 and 105.
7. The graph shown below is part of the parabola with equation $y=8 x-x^{2}$.

(a) By factorising $8 x-x^{2}$, find the roots of the equation

$$
8 x-x^{2}=0 .
$$

(b) State the equation of the axis of symmetry of the parabola.
(c) Find the coordinates of the turning point.
8. Given that

$$
\cos 60^{\circ}=0 \cdot 5
$$

what is the value of $\cos 240^{\circ}$ ?
9. A right-angled triangle is shown below.


Using Pythagoras' Theorem, find $x$.
Express your answer as a surd in its simplest form.
10. (a) Part of the graph of $y=\cos a x^{\circ}$ is shown below.


State the value of $a$.
(b) Part of the graph of $y=\tan b x^{\circ}$ is shown below.


State the value of $b$.
11. A straight line is represented by the equation $y=a x+b$.

Sketch a possible straight line graph to illustrate this equation when $a=0$ and $b>0$.

