## X101/204

NATIONAL
QUALIFICATIONS 2007

TUESDAY, 15 MAY
$2.05 \mathrm{PM}-3.35 \mathrm{PM}$

MATHEMATICS
INTERMEDIATE 2
Units 1, 2 and
Applications of Mathematics
Paper 2

## Read carefully

1 Calculators may be used in this paper.
2 Full credit will be given only where the solution contains appropriate working.
3 Square-ruled paper is provided.

Sine rule: $\quad \frac{a}{\sin \mathrm{~A}}=\frac{b}{\sin \mathrm{~B}}=\frac{c}{\sin \mathrm{C}}$

Cosine rule: $\quad a^{2}=b^{2}+c^{2}-2 b c \cos \mathrm{~A}$ or $\cos \mathrm{A}=\frac{b^{2}+c^{2}-a^{2}}{2 b c}$

Area of a triangle: $\quad$ Area $=\frac{1}{2} a b \sin \mathrm{C}$

Volume of a sphere: $\quad$ Volume $=\frac{4}{3} \pi r^{3}$

Volume of a cone: $\quad$ Volume $=\frac{1}{3} \pi r^{2} h$

Volume of a cylinder: Volume $=\pi r^{2} h$

Standard deviation: $\quad s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}=\sqrt{\frac{\sum x^{2}-\left(\sum x\right)^{2} / n}{n-1}}$, where $n$ is the sample size.

## ALL questions should be attempted.

1. Ian's annual salary is $£ 28400$. His boss tells him that his salary will increase by $2 \cdot 3 \%$ per annum.
What will Ian's annual salary be after 3 years?
Give your answer to the nearest pound.
2. The diagram below shows a sector of a circle, centre C.


The radius of the circle is 10.5 centimetres and angle ACB is $118^{\circ}$.
Calculate the length of arc AB.
3. This back-to-back stem and leaf diagram shows the results for a class in a recent mathematics examination.

|  |  |  | Girls |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | 1 | 3 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | 9 | 4 | 7 | 9 |  |  |  |  |  |  |  |
|  | 7 | 4 | 3 | 2 | 2 | 5 | 2 | 3 | 4 | 4 | 6 | 6 | 6 | 7 |  |
| 8 |  |  |  | 9 | 4 | 6 | 3 |  |  |  |  |  |  |  |  |
|  |  |  | 9 | 6 | 3 | 7 | 4 | 8 |  |  |  |  |  |  |  |
|  |  |  |  | 8 |  | 8 | 7 |  |  |  |  |  |  |  |  |

$$
\mathrm{n}=15 \quad \mathrm{n}=14
$$

$$
\begin{array}{l|l|l}
\text { Key } & \\
3 & \\
3 & \text { represents } 73 \% \\
& 8 & 7 \\
\text { represents } 87 \%
\end{array}
$$

(a) A boxplot is drawn to represent one set of data.


Does the boxplot above represent the girls' data or the boys' data?
Give a reason for your answer.
(b) For the other set of data, find:
(i) the median;
(ii) the lower quartile;
(iii) the upper quartile.
(c) Use the answers found in part (b) to construct a second boxplot.
(d) Make an appropriate comment about the distribution of data in the two sets.
4.


The tangent PQ touches the circle, centre O , at T .
Angle MTP is $77^{\circ}$.
(a) Calculate the size of angle MOT.
(b) The radius of the circle is 8 centimetres.

Calculate the length of chord MT.
5. A glass ornament in the shape of a cone is partly filled with coloured water.


The cone is 24 centimetres high and has a base of diameter 30 centimetres.
The water is 16 centimetres deep and measures 10 centimetres across the top.
What is the volume of the water?
Give your answer correct to 2 significant figures.
6. Tasnim rolls a standard dice with faces numbered 1 to 6 .

The probability that she gets a number less than 7 is
A 0
B $\quad \frac{1}{7}$
C $\frac{1}{6}$
D 1 .
Write down the letter that corresponds to the correct probability.
7. Factorise fully

$$
\begin{equation*}
2 x^{2}-18 \tag{2}
\end{equation*}
$$

8. A job as a sales consultant is advertised.


Matthew telephones for information and finds out that the basic wage is $£ 15000$. In addition to this he will receive $2 \cdot 5 \%$ commission on all his sales.

What value of sales will Matthew have to make in order to earn $£ 22000$ per year?
9. The diagram shows two blocks of flats of equal height.

$A$ and $B$ represent points on the top of the flats and $C$ represents a point on the ground between them.
To calculate the height, $h$, of each block of flats, a surveyor measures the angles of depression from A and B to C.

From A, the angle of depression is $38^{\circ}$.
From B, the angle of depression is $46^{\circ}$.
The distance $A B$ is 30 metres.

Calculate the height, $h$, in metres.
10. A network diagram is shown below.


State the order of node C.
11. The table below shows the monthly repayments to be made, with and without payment protection, when money is borrowed from the Good Deal Loan Company.

| $\begin{gathered} \text { loan } \\ \text { amount } \end{gathered}$ | 60 months |  | 48 months |  | 36 months |  | 24 months |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | W | WO | W | WO | W | WO | W | WO |
| £15000 | 342.63 | 288.49 | $409 \cdot 43$ | 350.79 | 510.76 | $454 \cdot 86$ | 736.73 | $663 \cdot 35$ |
| £12500 | 285.53 | $240 \cdot 41$ | 341-20 | $292 \cdot 33$ | $425 \cdot 63$ | 379.05 | 613.94 | 552.79 |
| $£ 10000$ | $228 \cdot 42$ | 192.33 | $272 \cdot 95$ | $233 \cdot 86$ | 340.50 | 303.24 | $491 \cdot 15$ | $442 \cdot 23$ |
| $£ 7500$ | 171.31 | 144.24 | 204.72 | $175 \cdot 40$ | $255 \cdot 38$ | 227-43 | 368.37 | 331.68 |
| $£ 5000$ | 114-21 | $96 \cdot 16$ | $136 \cdot 48$ | 116.93 | $170 \cdot 25$ | 151.62 | $245 \cdot 58$ | $221 \cdot 12$ |
| $\mathbf{W}=$ with payment protection |  |  |  | WO = without payment protection |  |  |  |  |

(a) Joseph decides to borrow $£ 12500$.

If he repays it over 48 months, without payment protection, calculate the cost of the loan.
(b) Brian thinks it would be cheaper to take a loan of $£ 12500$ over 36 months with payment protection.
Is he correct?
Explain your answer.
12. A mirror is shaped like part of a circle.


The radius of the circle, centre C , is 24 centimetres.
The height of the mirror is 35 centimetres.
Calculate the length of the base of the mirror, represented in the diagram by AB.
13. 28 students timed their journeys from home to college.

The results, in minutes, are listed below.

| 14 | 34 | 22 | 13 | 17 | 15 | 36 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 17 | 8 | 14 | 24 | 2 | 25 | 17 |
| 31 | 17 | 20 | 23 | 10 | 28 | 19 |
| 21 | 22 | 28 | 30 | 21 | 16 | 19 |

(a) Construct a frequency table for the above data using class intervals

$$
1-5, \quad 6-10, \quad 11-15, \quad \text { etc. }
$$

(b) Using the frequency table in part (a), calculate the mean number of minutes per journey.

