## Functions from Graphs

1. The diagram shows a parabola with equation $y=a x(x-b)$.

Find the values of $a$ and $b$.

2. The diagram shows a parabola with equation $y=k x(x-b)$.

Find the values of k and b .

3. The diagram shows a parabola with equation $y=a x(x-b)$.

Find the values of a and b .

4. The diagram shows a parabola with equation $y=k x(x+b)$.

Find the values of k and b .

5. The parabola opposite crosses the x -axis at $(0,0)$ and $(2,0)$ and has a minimum turning point at $(1,-6)$.

Find the equation of this parabola.

6. The parabola shown is of the form $y=a x(x-b)$. It has a maximum turning point of $(4,32)$ and $P$ is the point $(8,0)$.
(a) Find the equation of the parabola.
(b) The line $y=-2 x+16$ intersects this parabola at P and Q . Find the coordinates of Q .

7. (a) Find the equation of the parabola, $f(x)$, shown opposite.
(b) Find the coordinates of P .
(c) Hence calculate the shaded area.

8. The diagram shows the graph of $y=f(x)$. The graph is of the form $y=k x(x-b)$.
(a) Find a formula for $\mathrm{f}(\mathrm{x})$.
(b) Calculate the shaded area.

9. The diagram shows a parabola with equation $y=a x(x-b)$.
(a) Find the values of $a$ and $b$.
(b) $y=f^{\prime}(x)$. Find a formula for $f(x)$ given $f(3)=-4$.

10. A parabola passes through the points $(0,0),(6,0)$ and $(3,9)$ as shown.
(a) The equation of this parabola can be written in the form $y=a x(b-x)$. Find the values of $a$ and $b$.
(b) The line $y=x+4$ intersects this curve at two points . Find the coordinates of these points.

11. The diagram shows a parabola with equation $y=k(x-a)(x-b)$.
(a) Find the values of k , a and b .
(b) $y=f^{\prime}(x)$. Find a formula for $f(x)$ given $f(6)=-40$.

12. In the diagram A is the point $(1,12)$. Find the equation of $\mathrm{f}(\mathrm{x})$.

13. The function shown has zeros at $x=1,4$, and 6 . It has a maximum turning point at $(5,8)$.

Find the equation of this cubic function.

14. (a) The graph shown opposite crosses the x -axis at $(-1,0)$ and $(2,0)$ and has a maximum turning point of $(0,4)$.
Find the equation of this graph.
(b) P is the point $(3,14)$ and Q is $(-1,-10)$. Find the equation of the line PQ .
(c) The line PQ intersects the graph in (a) at 3 points. If one of these points is $(4,20)$ find the other points of intersection.

15. The diagram opposite is a sketch of the graph of a cubic function $y=f(x)$.
(a) If $\mathrm{y}=-16$ is a tangent to the curve,
find a formula for $\mathrm{f}(\mathrm{x})$.
(b) The line $\mathrm{y}=12 \mathrm{x}-32$ crosses this curve at 3 points.
Find the coordinates of these points.

16. (a) The parabola opposite cuts the x -axis at -1 and $p$ and the $y$-axis at $-2 p$. Show that the parabola has equation $y=2 x^{2}+2 x(1-p)-2 p$.
(b) The shaded area has a value equal to $\frac{-10 \mathrm{p}}{3}$.
Calculate the value of $p$.


