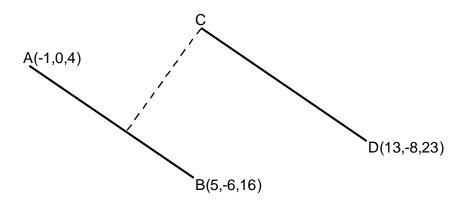
## **Vectors**

1. 
$$\mathbf{a} = \begin{pmatrix} 3 \\ -1 \\ 2 \end{pmatrix}$$
 and  $\mathbf{b} = \begin{pmatrix} -4 \\ 0 \\ 2 \end{pmatrix}$ .

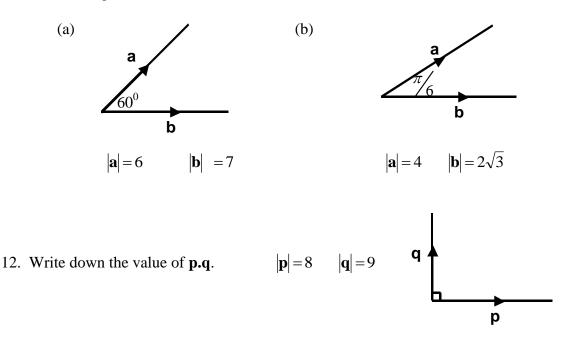
Calculate (a)  $|{\bf b}|$  (b)  $|2{\bf a} - {\bf b}|$  (c)  $|3({\bf a} + {\bf b})|$ 

- 2. (a) Find the magnitude of the vector  $\begin{pmatrix} \frac{1}{3} \\ -\frac{2}{3} \\ \frac{2}{3} \end{pmatrix}$ . (b) Find a vector parallel to the vector  $\begin{pmatrix} -4 \\ 3 \\ 0 \end{pmatrix}$  which has unit length.
- 3. A is (0,-3,5), B is (7,-6,9) and C is (21,-12,17). Show that A, B and C are collinear stating the ratio AB:BC.
- 4. PQRS is a parallelogram with P(3,4,0), Q(7,6,-3) and R(8,5,2). Find the coordinates of S.
- 5. (a) P is the point (-1,8,0) and Q is (4,-2,5). B divides PQ in the ratio 3:2. Find the coordinates of B.
  - (b) A is (0,1,5) and C is (8,5,-3). Show that A, B and C are collinear.
- 6. An aeroplane flies in a straight line at a constant speed. It takes 3 hours to fly from A to B and 4 hours to fly from B to C. Relative to coordinate axes, A is (0,-1,6) and C is (7,6,-1). Find the coordinates of B.
- 7.  $\mathbf{u} = 2\mathbf{i} 2\mathbf{j} + 4\mathbf{k}$  and  $\mathbf{v} = \mathbf{i} + 4\mathbf{j} + \sqrt{7}\mathbf{k}$ . If  $|\mathbf{u}| = |\mathbf{v}|$  find the value of a.
- 8. Show that the vectors  $\mathbf{a} = 2\mathbf{i} 4\mathbf{j} + 6\mathbf{k}$  and  $\mathbf{b} = 4\mathbf{i} 7\mathbf{j} 6\mathbf{k}$  are perpendicular.
- 9. A triangle has vertices A(6,-1,9), B(3,-2,11) and C(7,-8,14). Show that this triangle is right-angled at B.

10. Three points A, B and D have coordinates as shown.



- (a) Find the coordinates of C if AB is parallel and equal in length to CD.
- (b) The point E divides AB in the ratio 2:1, find the coordinates of E.
- (c) Prove that CE is perpendicular to AB.
- 11. Use the diagrams to find the value of **a.b**.



- 13. A triangle is formed from R(0,4,-1), S(1,5,2) and T(6,1,-2).
  - (a) Find the vectors  $\overrightarrow{RS}$  and  $\overrightarrow{RT}$ .
  - (b) Evaluate RS.RT
  - (c) What can you deduce about he lines RS and RT.

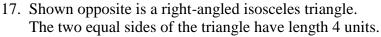
14. A, B, C and D are the points (-1,3,1), (1,6,7), (0,2,5) and (1,4,10) respectively.

- (a) Find the components of  $\overrightarrow{AB}$  and  $\overrightarrow{CD}$ .
- (b) The vector  $\begin{pmatrix} p \\ q \\ 1 \end{pmatrix}$  is perpendicular to both  $\overrightarrow{AB}$  and  $\overrightarrow{CD}$ . Find p and q.

15. 
$$\mathbf{u} = \begin{pmatrix} -3 \\ 3 \\ k \end{pmatrix}$$
 and  $\mathbf{v} = \begin{pmatrix} 1 \\ 5 \\ -1 \end{pmatrix}$ .

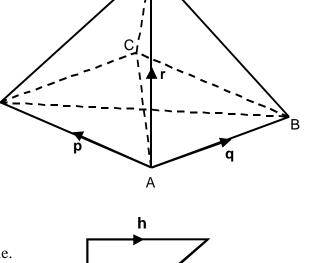
- (a) Write down the vectors  $\mathbf{u} + \mathbf{v}$  and  $\mathbf{u} \mathbf{v}$ .
- (b) Given that  $\mathbf{u} + \mathbf{v}$  and  $\mathbf{u} \mathbf{v}$  are perpendicular find k.
- 16. In the square based pyramid opposite all eight edges are of length 5 units.

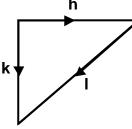
Evaluate  $\mathbf{p.}(\mathbf{q} + \mathbf{r})$ .

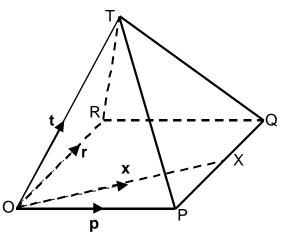


Find the value of  $\mathbf{k} \cdot (\mathbf{h} + \mathbf{k} + \mathbf{l})$ .

- In the diagram opposite TOPQR is a pyramid whose base OPQR is a rhombus of length 1 unit. OPT and ORT are equilateral triangles.
  - (a) Evaluate **t.r**.
  - (b) Given X is the midpoint of PQ, evaluate **t.x**.

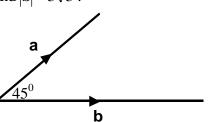


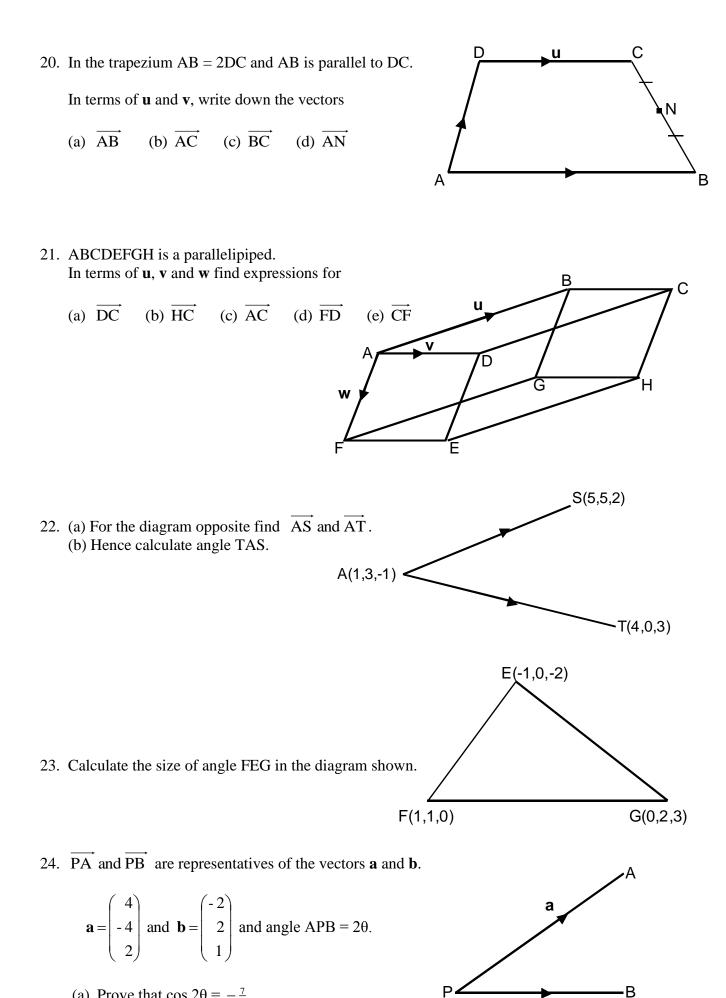




19. The diagram shows two vectors **a** and **b** with  $|\mathbf{a}| = 2$  and  $|\mathbf{b}| = 3\sqrt{3}$ .

- (a) Evaluate (a) **a.a** (b) **b.b** (c) **a.b**
- (b) Given  $\mathbf{p} = 2\mathbf{a} + 3\mathbf{b}$  evaluate **p.p**.





b

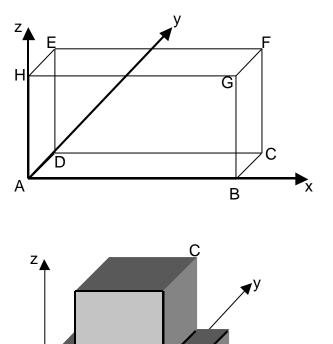
- (a) Prove that  $\cos 2\theta = -\frac{7}{9}$
- (b) Hence find the exact value of  $\cos^2\theta$ .

- 25. In the diagram AB = 15, BC = 6 and CF = 8
  - (a) Write down the coordinates of D and F
  - (b) Calculate the size of angle DBF.

26. The diagram shows three cuboids placed on top of each other.
Two of the cuboids are equal in size – 10 cm by 3 cm by 5 cm.
The third cuboid is centrally placed on the

other two and has dimensions 6 cm by 3 cm by 5 cm.

- (a) Write down the coordinates of A, B and C.
- (b) Calculate the size of angle BAC.



5

х

3

В

6

10