1. 
$$\mathbf{p} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$$
 and  $\mathbf{q} = \begin{pmatrix} 6 \\ -4 \end{pmatrix}$ 

- (a) Sketch the vectors **p** and **q**.
- (b) Sketch the vectors –**p** and –**q**.
- (c) Given  $\mathbf{u} = \mathbf{p} + \mathbf{q}$ , sketch the vector  $\mathbf{u}$ .
- (d) Given  $\mathbf{v} = \mathbf{p} \mathbf{q}$ , sketch the vector  $\mathbf{v}$ .

2. 
$$\mathbf{a} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$$
 and  $\mathbf{b} = \begin{pmatrix} -7 \\ -4 \end{pmatrix}$ 

- (a) Sketch the vectors **a** and **b**.
- (b)Given  $\mathbf{u} = \mathbf{a} + \mathbf{b}$ , sketch the vector  $\mathbf{u}$ .
- (c)Given  $\mathbf{v} = \mathbf{a} \mathbf{b}$ , sketch the vector  $\mathbf{v}$ .

3. 
$$\mathbf{a} = \begin{pmatrix} 2 \\ 2 \\ -1 \end{pmatrix}$$
 and  $\mathbf{b} = \begin{pmatrix} 6 \\ -8 \\ 0 \end{pmatrix}$ .

Find (a) 3a (b) -b (c) 2a + 3b (d) 4b - a (e)  $-\frac{1}{2}b$ (f) |b| (g) |2a| (h) |b+2a|

4. Find **p** and **q** in each equation below

(a) 
$$\begin{pmatrix} \mathbf{p} \\ \mathbf{q} \end{pmatrix} + \begin{pmatrix} 2 \\ -1 \end{pmatrix} = \begin{pmatrix} 6 \\ 4 \end{pmatrix}$$
 (b)  $\begin{pmatrix} \mathbf{p} \\ \mathbf{q} \end{pmatrix} - \begin{pmatrix} 3 \\ -4 \end{pmatrix} = \begin{pmatrix} 8 \\ -4 \end{pmatrix}$  (c)  $\begin{pmatrix} -3 \\ 1 \end{pmatrix} - \begin{pmatrix} \mathbf{p} \\ \mathbf{q} \end{pmatrix} = 3 \begin{pmatrix} -2 \\ -1 \end{pmatrix}$ 

5. Find **p**, **q** and **r** in each of the following

(a) 
$$\begin{pmatrix} \mathbf{p} \\ \mathbf{q} \\ \mathbf{r} \end{pmatrix} + \begin{pmatrix} 3 \\ -2 \\ 5 \end{pmatrix} = \begin{pmatrix} 6 \\ 4 \\ 1 \end{pmatrix}$$
 (b)  $\begin{pmatrix} \mathbf{p} \\ \mathbf{q} \\ \mathbf{r} \end{pmatrix} + 2 \begin{pmatrix} 1 \\ -4 \\ 0 \end{pmatrix} = \begin{pmatrix} 2 \\ 5 \\ 3 \end{pmatrix}$ 

6. A is the point (2,1,-2) and B is the point (0,-3,4).

(a) Write down the components of **a** and **b**, the position vectors of A and B.

- (b) Calculate (i)  $-2\mathbf{a} + \mathbf{b}$  (ii)  $|-2\mathbf{a} + \mathbf{b}|$
- (c) Find the vector AB
- 7. P is the point (1,-1,2), Q is (2,0,-5) and R is (1,1,0).
  - (a) Write down the components of **p**, **q** and **r** the position vectors of **P**, **Q** and **R**.
  - (b) Find the vectors (i)  $\overrightarrow{QP}$  (ii)  $\overrightarrow{QR}$  (iii)  $\overrightarrow{PR}$

- 8. M is the point (2,3,-5), N is (1,1,0) and R is (-4,2,-2).
  - (a) Write down the components of **m**, **n** and **r** the position vectors of M, N and R.
  - (b) Find the vectors (i)  $\overline{MN}$  (ii)  $\overline{RN}$  (iii) MR
- 9. PQRS is a parallelogram with vertices P(3,4,0), Q(7,6,-3) and R(8,5,2). Find the coordinates of S. (Hint:  $\overrightarrow{PQ} = \overrightarrow{SR}$ ).
- 10. A is the point (2,1,-6), B is (3,1,-9) and C is (0,1,6). Given  $\overrightarrow{AD} = \frac{2}{3}\overrightarrow{BC}$ , find the coordinates of D.
- 11. P is the point (-4,2,2), Q is (-1,8,14) and R is (-5,2,10). Given  $\overrightarrow{PQ} = \frac{3}{4}\overrightarrow{RS}$ , find the coordinates of S.

12. (a) Calculate the magnitude of the vector  $\mathbf{u} = \begin{pmatrix} 3 \\ 4 \end{pmatrix}$ .

(b) Find a unit vector parallel to the vector **u**.

- 13. (a) Calculate the magnitude of the vector  $\mathbf{w} = \begin{pmatrix} -6\\2\\3 \end{pmatrix}$ 
  - (b) Find a unit vector parallel to **w**.

14. (a) Calculate 
$$|\mathbf{a}|$$
 where  $\mathbf{a} = \begin{pmatrix} -2 \\ -1 \\ 0 \end{pmatrix}$ 

(b) Find a unit vector parallel to **a**.

15. The diagram shows a regular hexagon.

(i) Write down another vector equal to (a)  $\overrightarrow{AB}$  (b)  $\overrightarrow{CD}$ 

(ii) Find a vector equal to

(a)  $\overrightarrow{AB} + \overrightarrow{BC}$  (b)  $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD}$  (c)  $\overrightarrow{FE} + \overrightarrow{ED}$ 





- 16. Use the diagram opposite to name the vector that represents
  - (a) p-r (b) r-p (c) t-q (d) s-t(e) p-r-q (f) t+r-p (g) s-p+q



R

S

- 17. The diagram shows a regular octagon.
  - (a) Write down another vector equal to
    - (i)  $\overrightarrow{WP}$  (ii)  $\overrightarrow{WV} + \overrightarrow{VU}$ (iii)  $\overrightarrow{WP} + \overrightarrow{SR} + \overrightarrow{RQ}$  (iv)  $\overrightarrow{SR} - \overrightarrow{ST}$



W

V

U

- 18. The diagram shows a cuboid ABCD EFGH.
  - (a) Express in terms of **u**, **v** and **w**.
    - (i)  $\overrightarrow{DC}$  (ii)  $\overrightarrow{ED}$
    - (iii)  $\overrightarrow{FH}$  (iv)  $\overrightarrow{HA}$
  - (b) Express in terms of ABCD EFGH

(i)  $\mathbf{u} + \mathbf{v}$  (ii)  $\mathbf{u} - \mathbf{w}$  (iii)  $\mathbf{w} - \mathbf{u} + \mathbf{v}$ 

- 19. In the trapezium AB = 2DC and AB is parallel to DC. In terms of **u** and **v**, write down the vectors
  - (a)  $\overrightarrow{AB}$  (b)  $\overrightarrow{AC}$  (c)  $\overrightarrow{BC}$  (d)  $\overrightarrow{AN}$

